The Physics & Astrophysics of Cosmic Rays

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What are Cosmic Rays?

A non-thermal population of relativistic particles that pervade the solar system, galaxies, clusters and intergalactic space

Why you Should Care about Cosmic Rays

- Beautiful physics: nuclear physics, high energy physics, plasma physics ...
- An energetically important component of galaxies, clusters, etc.
- Relativistic particles dominate the emission in many wavebands
- Cosmic rays have amazing/surprising/poorly understood properties that can confound attempts at indirect detection of dark matter

Outline

- An Overview of Cosmic Rays in the Galaxy
- The Physical Origin of Cosmic Rays
 - Galactic: Shock Acceleration in Supernovae
- Ultra-High Energy Cosmic Rays: Extragalactic Sources
- The Confinement of Cosmic Rays
- Cosmic Ray (Magneto)Hydrodynamics
- Applications: Galaxies & Clusters
- Open Problems



Composition

mostly protons at $\lesssim 10^{15} \text{ eV}$ (*lots* of detailed composition info)

some indication of heavier nuclei at $E \gtrsim 10^{18} \text{ eV}$



Larmor Radius

 $r_L = E/ZeB$

 $r_L \simeq 10 \,\mathrm{kpc} \frac{E/(10^{17} \,\mathrm{eV})}{Z(B/1\mu G)}$

GeV Coulomb mfp ~10³ n⁻¹ D_{Horizon}

Interaction with EM Fluctuations Govern CR Motion



Ion Spectra & Energetics

 $\frac{dN}{dE} \propto E^{-2.7}$

 $\frac{dF_E}{d\ln E} \propto E^{-0.7}$

most of the energy is in ~GeV CR protons

energy density near Earth ~ 2×10⁻¹² erg cm⁻³ ~ eV cm⁻³

Electrons & Positrons



e/p ~ 0.02 at ~ GeV $\frac{dN}{dE} \propto E^{-3.1}$ $\frac{dF_E}{d\ln E} \propto E^{-1.1}$

e⁺/e⁻ spectrum steeper than protons bec. of radiative losses (synchrotron & inverse Compton)

Force Balance in Galaxies: CRs and Magnetic Fields are Important!



Galactic Disk w/ Gas Surface Density Σ_g

Hydrostatic Equil: $P_{midplane} \sim \pi G \Sigma_g^2$ (+ DM, stellar contribution) Milky Way: $P_{midplane} \sim 4 \ 10^{-12} \ erg \ cm^{-3}$ roughly equal contributions from CRs, B-fields, gas turbulence (unclear whether this extends to other galaxies, in particular with galactic winds — more later)

Why P_{CR} ~ P_B ~ P_{Gravity}?

Rough Idea: B-field & CR Energy Build Up Until they are Dynamically Important ~ P_{Gravity} Then B-field/CRs are Unstable



Normal Spirals: Synchrotron (B-field, CR) scale-heights ~kpc > H_{gas} ~ 200 pc

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Rough Idea: B-field & CR Energy Build Up Until they are Dynamically Important ~ P_{Gravity} Then B-field/CRs are Unstable



Unstable if $\frac{d}{dz} \left(\frac{B^2}{\rho^2}\right) < 0$

(neglects gas/CR pressure)

Confinement Time

(Milky Way CRs Near the Sun)

• ¹⁰Be: CR with 1/2 life of 1.6 10⁶ yrs. Abundance compared to ⁷Be & ¹⁰Be \Rightarrow

$$t_{esc} \simeq 3\,10^7 \text{ yrs } \left(\frac{E}{3\,\text{GeV}}\right)^{-1/2} \ll \text{kpc}/c \sim 3000 \text{ yrs}$$

• If diffusion:
$$t_{esc} \sim \frac{R^2}{\ell c} \Rightarrow$$

$$\min f \ell \sim 0.1 \operatorname{pc} \left(\frac{E}{3 \operatorname{GeV}}\right)^{1/2}$$

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- Abundance of spallation products Be, B, Li \Rightarrow
 - CRs traverse a column density $\Sigma_g \approx 5 \text{ g cm}^{-2} (\text{E/3 GeV})^{-1/2}$
 - CRs interact with gas density $\approx \sum_g /(c t_{esc} m_p) \approx 0.1 \text{ cm}^{-3}$

• << $n_{avg} \approx 1$ cm⁻³: inhomogeneous ISM; CR scale-height >> gas scale-height

Inferences from Confinement Time Measurements

Injection Spectrum ≠ Measured Spectrum

$$\frac{dN}{d\ln E} \simeq \frac{d\dot{N}}{d\ln E} t_{esc}(E) \qquad \frac{d\dot{N}}{d\ln E} \propto E^{-2.2}$$
roughly equal energy injected per decade in energy: $\frac{d\dot{F}_E}{d\ln E} \sim \text{const}$
• For e⁺/e⁻ synchrotron/IC cooling dominates
$$t_{\text{synch}} \simeq 3 \times 10^7 \text{ yrs} \left(\frac{B}{6\mu G}\right)^{-2} \left(\frac{E}{3 \text{ GeV}}\right)^{-1}$$

$$\frac{dN}{d\ln E} \simeq \frac{d\dot{N}}{d\ln E} t_{synch}(E) \qquad \frac{d\dot{N}_e}{\ln E} \propto E^{-2.1}$$

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Fermi Acceleration



$$\frac{\Delta E}{E} = 4\frac{u}{v}Cos\theta + 4\frac{u^2}{v^2}$$

(interested in rel. particles with v >> u)

random scatterers: $<\cos\Theta > = 0$

 $\Delta E/E \sim u^2/v^2$ (2nd order Fermi accel) converging flow: <Cos Θ > = I

 $\Delta E/E \sim u/v$ (1st order Fermi accel)

Fermi Acceleration

competition between acceleration (t_{acc}) and escape (t_{esc})

$$\frac{dE}{dt} = \frac{E}{t_{acc}} \qquad \frac{\partial N(E)}{\partial t} + \frac{\partial}{\partial E} \left(N(E) \frac{dE}{dt} \right) = -\frac{N(E)}{t_{esc}}$$

steady state: particles are injected, accelerated, and escape

$$N(E) \sim E^{-\alpha} \quad \alpha = I + t_{acc}/t_{esc}$$

power-law X but need t_{acc}/t_{esc} ~ I to explain CR spectrum??

(Bell 1978; Blandford & Ostriker 1978)



(Bell 1978; Blandford & Ostriker 1978)



(Bell 1978; Blandford & Ostriker 1978)



downstream (shocked)

upstream frame upstream (unshocked)

(Bell 1978; Blandford & Ostriker 1978)



(Bell 1978; Blandford & Ostriker 1978)



downstream (shocked)

downstream frame upstream (unshocked)

First Order Fermi Acceleration at Shocks (given sufficient turbulence to scatter particles)



(Bell 1978; Blandford & Ostriker 1978)



Inferences from Confinement Time Measurements

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Shock Acceleration in Particlein-Cell Plasma Simulations

Self-generated magnetic turbulence scatters particles across the shock; each crossing results in energy gain -- Fermi process

Magnetic filaments





Slide Courtesy of Anatoly Spitkovsky

Galactic Cosmic Rays From Supernova Shocks

• $\epsilon_{CR} \sim 2 \ 10^{-12} \, erg \, cm^{-3}$ $t_{esc} \sim 3 \ 10^7 \, yr$ $V_{CR} \sim \pi (10 \, kpc)^2 (2kpc)$

$$\dot{E}_{CR} \simeq 10^{41} \,\mathrm{erg} \,\mathrm{s}^{-1} \simeq 0.1 \,\dot{E}_{SN} \left(\frac{\dot{M}_*}{3 \,M_{\odot} \,yr^{-1}}\right)$$

Supernova W44 & IC 443 Neutral Pion Decay Spectral Fit



 $\begin{array}{c} CR p + p \\ \rightarrow \pi_0 \rightarrow \gamma \end{array}$



Larmor Radius

 $r_L = E/ZeB$

 $r_L \simeq 1 \operatorname{pc} \frac{E/(10^{15} \text{ eV})}{Z(B/100\mu G)}$

SN shocks cannot accelerate particles with $r_L \gtrsim$ size of remnant ~ few pc \rightarrow $E_{CR} \lesssim 10^{15} \text{ Z eV}$

The Range of Injection Energy Spectra

 strong shocks give dF_E/dlnE ~ const but can get a wider range of spectral slopes from other mechanisms



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What Sources Satisfy $r_L < System Size at ~10^{20} eV$?



Plausible Sources

AGN (Jets, Lobes) Cluster Virial Shocks Gamma-ray Bursts

Above ~ $10^{19.5}$ eV sources must be $\lesssim 50$ Mpc due to CMB + CR $\rightarrow \pi$ + CR (GZK cutoff)

But anisotropy in UHECR arrival directions with Auger is weak

Composition of UHECRs



Composition Dependent Properties of Air Showers From Pierre Auger Observatory Suggest Heavy Nuclei at $\gtrsim 10^{19} \text{ eV}$

Connection to High Energy Neutrinos From Ice Cube



Sources of high energy CR expected to produce Vs via p-p and/or photo-meson interaction

$CR p + p \rightarrow \pi_{+/-} \rightarrow e_{+/-} + v$



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• If diffusion:
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$$\min f \ell \sim 0.1 \operatorname{pc} \left(\frac{E}{3 \operatorname{GeV}}\right)^{1/2}$$

Why it is Critical to Understand tesc

steady state energy density $\sim \dot{E} t_{esc}$

- We don't understand the right function to use for tesc in difft environments (high z galaxies, clusters)
 - t_{esc} plausibly depends on E_{CR} , B, n, δv , ionization state, ...
- We don't understand whether 'escape' should be modeled as diffusion or advection or ...
- Less severe for e- bec. radiative losses often rapid and $\epsilon_e \sim \dot{E} t_{cool}$ (but protons dominate CR energy!)

Physics of CR Confinement

- GeV Coulomb mfp ~10³ n⁻¹ D_{Horizon} →
 Interaction w/ EM Fields Governs CR Motion
- Charged Particle Motion in a Varying B-Field
- Scattering by Cyclotron-Frequency Waves
- Scattering by MHD Turbulence
- Self-Confinement CRs 'trying' to stream at the speed of light generate instabilities that limit CR streaming to ~ Alfven speed

Charged Particle Motion in a Slowly Varying Magnetic Field



Scattering by High Frequency MHD Waves

 High frequency ~ Ω (cyclotron freq) fluctuations in B can scatter particles, converting p⊥ ⇔ P||, much like standard collisions. This sets CR mfp.



if $\omega - k_z v_z = \Omega$ particle is in resonance and sees constant wave amplitude

for rel particles, resonance if $\lambda_{\parallel} \sim 1/k_z \sim r_L$

Scattering by High Frequency MHD Waves

 High frequency ~ Ω (cyclotron freq) fluctuations in B can scatter particles, converting p⊥ ⇔ P||, much like standard collisions. This sets CR mfp.

rate of
$$p_{\perp} \Leftrightarrow p_{\parallel}$$

scattering for
randomly phased
resonant waves

$$\nu_s \sim \Omega\left(\frac{\delta B}{B_0}\right)^2 \qquad \text{CR mfp } \ell = c/\nu_s$$

if diffusion, the inferred CR mfp ℓ ~ 0.1 pc at ~ GeV

requires $\delta B/B_0 \sim 10^{-3}$ at $\lambda_{||} \sim r_L \sim 10^{12}$ cm

Scattering by MHD Turbulence

- Magnetized Turbulence is Ubiquitous in the ISM with $\delta B/B_0 \sim I$ at the outer (driving) scale L_{out}
- Let's very naively say δB₀ ~ k^{-1/3} as in hydrodynamic turbulence (Kolmogorov)
- $L_{out} \sim 100 \text{ pc} \rightarrow \delta B/B_0 \sim 10^{-3} \text{ at } \lambda \sim 10^{12} \text{ cm}$, comparable to what we inferred is needed
- But reality is more complicated

Scattering by MHD Turbulence

- MHD Turbulence can be Roughly Decomposed into the 3 MHD Waves: slow, fast, Alfven
- Alfven, slow turbulence anisotropic wrt B-field



'eddies' elongated along mean B-field: λ⊥ << λ||
 when λ|| ~ rL of CR, λ⊥ << rL;
 strongly suppresses CR scattering
 bec of averaging over many eddies
 → Alfven/slow modes are an
 inefficient source of scattering

Scattering by MHD Turbulence

- MHD Turbulence can be Roughly Decomposed into the 3 MHD Waves: slow, fast, Alfven
- fast mode (~sound wave w/ B-field compressions) turbulence isotropic wrt B-field

 $\delta B \sim k^{-1/4}$ waves with $\lambda \sim r_L \rightarrow CR mfp \sim c L_{out}^{1/2} \Omega^{1/2} \sim E^{1/2}$ as observed



fast modes are strongly damped but nonetheless may be the dominant source of CR scattering by ambient turbulence

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What do we know about Magnetic Fields and CRs in Galaxies from their Non-thermal Emission? (based on Thompson+ 2006, 2007; Lacki+ 2010, 2011)

 Constraints primarily for star-forming galaxies in which core-collapse supernova rate is large (>> la rate)

• Synchrotron (radio) emission from star-forming galaxies

- Implications for B-fields in star-forming galaxies
- The Far-infrared-radio (FIR) correlation of star-forming galaxies
- Gamma-ray emission from starbursts
 - Suggests CR pressure is sub-dominant in prototypical starbursts M82, NGC 253

The FIR-Radio Correlation



(at ~ few GHz, where the radio emission is nonthermal)



Estimating B-Field Strengths in Other Galaxies

- Very few Zeeman detections in other galaxies
- Use observed radio emission (synchrotron) to estimate B
- Two Observables: L_{rad} & R (+ radio spectrum)
 - e.g., Arp 220 (L_{FIR} ~ 10¹² L_{\odot}):

 $L_{rad} \sim 10^{40} \, ergs/s \& R \sim 100 \, pc$



$\begin{array}{ll} \mbox{The Minimum Energy Estimate} \\ P\propto\gamma^2B^2 & t_{syn}\sim 10^9 B_{\mu G}^{-3/2} \nu_{GHz}^{-1/2} ~{\rm yr} ~~ \gamma\sim 10^4 \nu_{GHz}^{1/2} B_{\mu G}^{-1/2} \end{array}$

$$\nu L_{\nu} \sim \frac{\epsilon_e V}{t_{syn}} \propto \epsilon_e V B^{3/2}$$

assume
$$\epsilon_{tot} = \delta \epsilon_e \sim \frac{B^2}{8\pi}$$
 ($\delta \equiv p/e \ CR \ energy \sim 10 - 100$)
 $\rightarrow \nu L_{\nu} \propto \delta^{-1} B^{7/2} V$ $\Rightarrow \mathbf{B} \equiv \mathbf{B}_{\min} \propto \delta^{2/7} \left(\frac{\mathbf{L}_{\nu}}{\mathbf{V}}\right)^{2/7}$

(minimum energy bec. $\epsilon_{tot} + B^2/8\pi$ minimized by $\epsilon_{tot} \sim B^2/8\pi$)

Milky Way: B_{min} ~ 5 μG, consistent with Faraday Rot. $ε_{tot} ~ B^2/8π$ confirmed by γ-ray observations (pion decay from p-p interactions)

The Minimum Energy Magnetic Field From Local Spirals to Luminous Starbursts

if B_{min} is correct, B-fields are dynamically weak compared to gravity in starbursts

(and thus likely unimpt. in regulating star formation, transporting angular momentum, ...)



The Failure of the Min. Energy Estimate

• $\varepsilon_e << B^2/8\pi$ if

t_{cool} << t_{esc}

time for rel. eto radiate away its energy (synch & IC)

time for rel eto escape the galactic disk

- if $t_{cool} \ll t_{esc}$, B >> B_{min}
 - − $L_{radio} \sim ε_e B^{3/2}$: $ε_e \downarrow \Rightarrow B \uparrow$
- MW: $t_{syn} \sim t_{IC} \sim t_{esc} \sim 10^{7.5} \text{ yr}$
- Arp 220: t_{syn} ~ ? (B ~ ?) t_{IC} ~ 5000 yr t_{esc} ~ ?; t_{esc} > R/v_w~ 3 10⁵ yr



Implications of $t_{syn} < t_{esc}$

t_{syn} < t_{esc}: e's radiate all the energy supplied by SN shocks

$$u \mathbf{L}_{\nu} \sim \dot{\mathbf{E}}_{\mathbf{e}} \propto \mathrm{SN} \ \mathrm{Rate} \propto \mathbf{L}_{\mathbf{FIR}}$$

normalization of FIR-Radio $\rightarrow \approx 1\%$ of SN energy supplied to CR e's

Clean explanation for linear FIR-Radio Correlation

- "calorimeter theory" (Volk 1989; Thompson+2006)
- $t_{esc} < t_{syn}$ requires tremendous fine tuning and even more energy \rightarrow e- in SN shocks



Log₁₀[L_{FIR}

Synchrotron vs. IC cooling

- Conditions in Starbursts & FIR-Radio favor t_{cool} < t_{esc}
 - B_{min} is an underestimate

FIR-Radio also Requires
 t_{syn} < t_{IC}, i.e., U_B > U_{ph}





Thompson+2006

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Gamma-ray emission from starbursts

• Suggests CR pressure is sub-dominant in prototypical starbursts M82, NGC 253

Gamma-ray Emission from Starbursts

- Largest flux \geq GeV via neutral pion decay (m_{\pi}c² ~ 140 MeV)
 - e- IC, bremsstrahlung can also contribute (but ps have more energy)

$$CR p + p \rightarrow \pi_0 \rightarrow \gamma$$
$$t_{\text{pion}} \simeq 10^5 \text{ yrs } \left(\frac{n}{10^3 \text{ cm}^{-3}}\right)^{-1}$$

• $t_{pion} < (?) t_{esc}$ in dense starbursts \rightarrow 'proton calorimeter'

$$L(\gtrsim \text{GeV}) \simeq 2 \times 10^{-4} \left(\frac{\eta_p}{0.1}\right) L_{\text{FIR}}$$

(prediction by TQW 2007, prior to launch of Fermi)

a GeV-FIR correlation

Gamma-ray Emission from Starbursts



Gamma-ray Emission from Starbursts



Lacki+2011

High Density Star Forming Galaxies are a Significant Contributor to the Extragalactic Gamma-ray and Neutrino Backgrounds



Sources of high energy CR expected to produce Vs and γ via p-p interaction $CR p + p \rightarrow \pi_0 \rightarrow \gamma$ $CR p + p \rightarrow \pi_{+/-} \rightarrow e_{+/-} + v$



~28 ~PeV (10¹⁵ eV) vs

Implications for CR Pressure & Galactic Winds

 Given large ≥ GeV fluxes, need to account for pion losses in determining steady state CR energy ε_{CR}

 $\epsilon_{CR} \sim \dot{\epsilon}_{CR} \operatorname{Min}(t_{\text{pion}}, t_{\text{esc}}) \lesssim \dot{\epsilon}_{CR} t_{\text{pion}}$

- Best applied in prototypical starbursts M82 & NGC 253
 - Assume CRs interact with gas at $n_{eff} \sim \langle n \rangle \sim 300 \text{ cm}^{-3}$

• \rightarrow P_{CR} ~ 0.05 P_{Hydro} (P_{Hydro} = $\pi G \Sigma_g^2$) \rightarrow CRs subdominant

• Estimate n_{eff} such that $P_{CR} \sim P_{Hydro} \rightarrow n_{eff} \sim 10 \text{ cm}^{-3}$

$$t_{
m pion} \sim 10^7 {
m yrs} \gg rac{R}{v_{
m wind}} \sim 10^6 {
m yrs} \, \left(rac{R}{300 \, {
m pc}}
ight) \left(rac{300 \, {
m km \, s^{-1}}}{v_{
m wind}}
ight) \qquad {
m ruled \ out \ by} \ {
m large \ GeV \ flux}$$

Suggests that CRs are not driving the winds in NGC 253 and M82

(Lacki+2011)