

Worksheet Solutions Lecture 7

1 Worksheet

Solve:

$$\frac{p-7}{12} = -10 \quad (1)$$

$$p - 7 = -120$$

$$p = -113$$

$$9z - 45 = 45 \quad (2)$$

$$9z = 90$$

$$z = 10$$

$$9z - 4z + 4 = 24 \quad (3)$$

$$5z + 4 = 24$$

$$5z = 20$$

$$z = 4$$

$$3n + 5 + 12n = 35 \quad (4)$$

$$15n + 5 = 35$$

$$15n = 30$$

$$n = 2$$

$$-2(x + 6) = 32 \quad (5)$$

$$-2x - 12 = 32$$

$$-2x = 44$$

$$x = -22$$

$$3(x + 2) = 4 - x \quad (6)$$

$$3x + 6 = 4 - x$$

$$4x + 6 = 4$$

$$4x = -2$$

$$x = -\frac{1}{2}$$

$$n + 3 > 12 \quad (7)$$

$$n > 9$$

$$2(x - 4) < -4x \quad (8)$$

$$2x - 8 < -4x$$

$$6x < 8$$

$$x < \frac{4}{3}$$

$$-4x > 20 \quad (9)$$

$$x < -5$$

$$6(x + 2) - 8x > 6 + x \quad (10)$$

$$6x + 12 - 8x > 6 + x$$

$$-2x + 12 > 6 + x$$

$$-3x + 12 > 6$$

$$-3x > -6$$

$$3x < 6$$

$$x < 2$$

Translate into an equation:

1. **The sale price of \$125 for the camera is \$5 less than one third of the original price.**

p =original price

$$\frac{1}{3}p - 5 = 125$$

2. **The 468 students in the school are six less than 22 times the number of students taking algebra.**

n =number of students taking algebra

$$22n - 6 = 468$$

3. **Rachel's current salary, \$50 per week, is twice her starting salary increased by \$10.**

s =starting salary

$$2(s + 10) = 50$$

4. **The 37 students on the bus are three times the number in the van increased by three.**

v =number of students in the van

$$3(v + 3) = 37$$

5. **Eight times an integer n is less than 48.**

$$8n < 48$$

6. **The number of pebbles on the beach is at least five times greater than the number of trees in the forest.**

p =number of pebbles, t =number of trees

$$p \geq [5t]$$

Write the appropriate equation and solve:

1. **Eve bought 3 tickets to a play. She paid \$29 for the tickets, including a \$2 tax. Find the price of each ticket.**

Let t be the price of a single ticket.

$$3t + 2 = 29$$

$$3t = 27$$

$$t = 9$$

2. **The cost of grapefruits is 25% *more* this week than it was last week. If the price of grapefruits is \$5 this week, what was the price last week?**

Let p represent the price of grapefruits last week.

$$p + \frac{1}{4}p = 5$$

$$\frac{5}{4}p = 5$$

$$p = 5\left(\frac{4}{5}\right)$$

$$p = 4$$

3. **The cost of grapefruits is 25% *less* this week than it was last week. If the price of grapefruits was \$3 last week, what is the price this week?**

Let p represent the price of grapefruits this week.

$$p - \frac{1}{4}p = 3$$

$$\frac{3}{4}p = 3$$

$$p = 4$$

4. **The equation for the perimeter of a rectangle is that the perimeter P is the sum of twice the length l and twice the width w , or $P = 2l + 2w$. If the length of a field is 10m and the width is 5m, what is the perimeter.**

Here we will just substitute $l=10$ and $w=5$.

$$P = 2 \times 10 + 2 \times 5$$

$$P = 20 + 10$$

$$P = 30$$

5. **Another perimeter problem. If 50m of wire are needed to build a fence for a 9m wide rectangular field, how long is the field?**

This problem is a bit more complicated. We are told the WIDTH of the field, and the PERIMETER but we want to solve for the length. Let us call it l .

We know that $P = 2l + 2w$

We also know that $P = 50$ and that $w = 9$.

$$2 \times 9 + 2l = 50$$

$$2l = 32$$

$$l = 16$$

6. **One hour ago it was three times as long after noon as it was until midnight. What time is it?**

For simplicity, let's think of twelve noon as 0 hrs and 12 midnight as 12 hours. We will take t as the time now. Then one hour ago was $t - 1$.

$$(t - 1) = 3[12 - (t - 1)]$$

$$t - 1 = 3(12 - t + 1)$$

$$t - 1 = 36 - 3t + 3$$

$$4t - 1 = 39$$

$$4t = 40$$

$$t = 10$$

Note, we could have solved instead for the time ONE HOUR AGO, let us call that

$$x = t - 1.$$

$$x = 3(12 - x)$$

$$x = 36 - 3x$$

$$4x = 36$$

$$x = 9$$

$$t = x + 1 = 10$$