

Protostars and Pre-Main Sequence Evolution

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- Protostars

 - Gravitational Collapse

 - Accretion Phase

 - Comparisons to Observations

- Pre-Main Sequence Evolution

 - Convective and Radiative Contraction

 - Deuterium Burning and the Stellar Birth Line

 - Lithium Burning and Substellar Objects

 - Degeneracy

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- Conclusions

Bonnor-Ebbert Mass

$$M_{\text{crit}} = 1.18 \frac{c_s^4}{P_{\text{surf}}^{1/2} G^{3/2}} = 1.82 \left(\frac{n}{10^4 \text{cm}^{-3}} \right)^{-1/2} \left(\frac{T}{10 \text{K}} \right)^{3/2} M_{\odot}$$

The process starts with cores of $M \sim M_{\odot}$, and $R \sim 0.1$ pc.

Three phases of collapse

- Isothermal Collapse

- Adiabatic Collapse

- Envelope Accretion

Protostars

Isothermal and Adiabatic Collapse

$$\frac{Gm}{4\pi r^4} + \frac{dP}{dm} = -\frac{1}{4\pi r^2} \frac{d^2 r}{dt^2}, \quad L_r = -\frac{64\pi^2 a c r^4}{3\kappa_R} T^3 \frac{dT}{dm}$$

$$\frac{dr}{dm} = \frac{1}{4\pi r^2 \rho}, \quad \frac{dL_r}{dm} = -\frac{dE}{dt} - P \frac{dv}{dt}$$

with bc: $r = L_r = 0$ at $m = 0$, $P = P_0$, $L_R = 4\pi R^2 \sigma T_{\text{eff}}^4$ at $m = M$

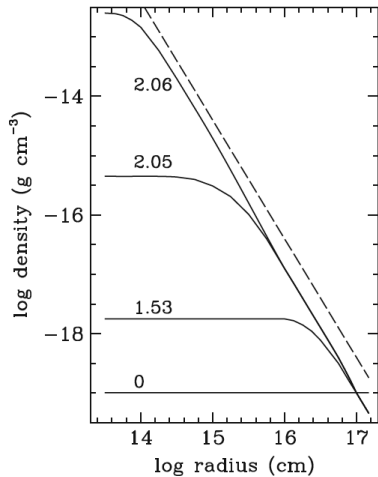
$$\tau \approx \kappa_R \rho R, \quad t_{\text{diff}} \approx 3\kappa_R \rho (\Delta r)^2 / c, \quad t_{\text{ff}} \approx (G\rho)^{-1/2}$$

Isothermal Phase: $\tau \ll 1$, $\rho = 10^{-19} - 10^{-13} \text{gcm}^{-3}$, efficient cooling, can assume constant temperature ($T \approx 10 \text{ K}$).

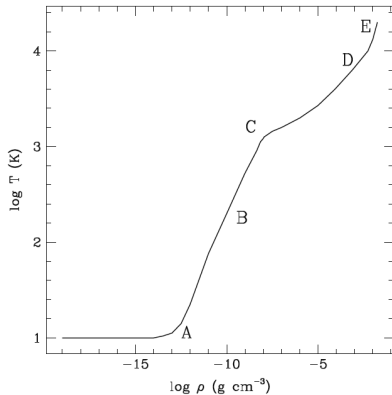
Adiabatic Phase: $\tau \gtrsim 1$, $t_{\text{diff}} \gg t_{\text{ff}}$, infrared radiation gets trapped, can ignore heat term in energy equation.

Protostars

Isothermal and Adiabatic Collapse



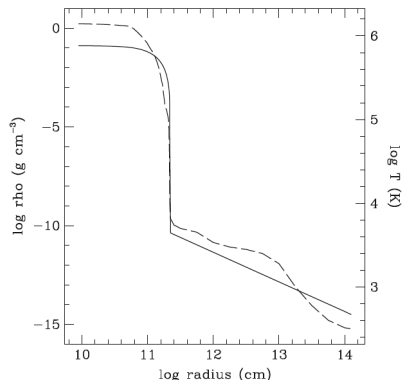
Larson, 1969



Bodenheimer, 2011

Protostars

Accretion Phase



Stahler et al., 1980

The central part of the core reaches *quasi-hydrostatic* equilibrium while the outer regions are still in isothermal collapse.

$$t_{\text{KH}} \approx GM^2/RL \sim \text{Myr}$$

$$t_{\text{acc}} \approx M/\dot{M} \sim 10^5 \text{ yr}$$

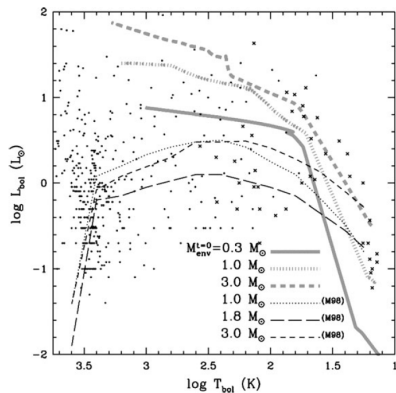
$t_{\text{diff}} \ll t_{\text{acc}} \ll t_{\text{KH}}$, therefore

$$L \approx L_{\text{acc}}.$$

Dust sublimates at $T \approx 1500 \text{ K}$.

Protostars

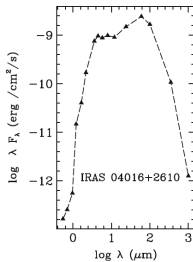
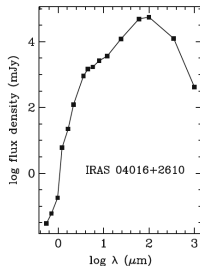
Comparisons to Observations



Bodenheimer, 2011

Luminosity Problem, for $M = 0.5 M_{\odot}$

$L_{\text{acc}} \sim 10 L_{\odot}$.



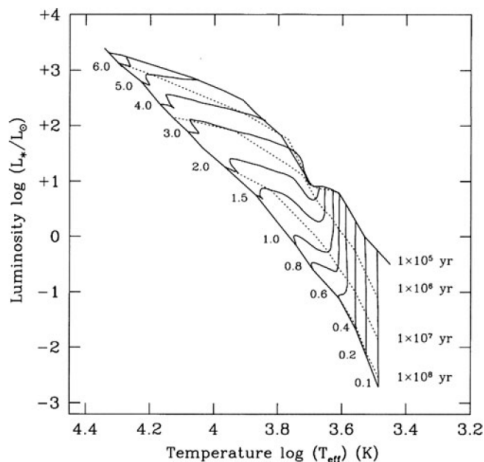
Kenyon et al., 1993

Bodenheimer, 2011

Non-thermal spectrum due wavelength dependent opacity.

Pre-Main Sequence Evolution

Convective and Radiative Contraction



Palla & Staller, 1999

In the interior,

$$\frac{3}{16\pi Gac} \frac{\kappa_R L_r P}{mT^4} > \left(\frac{\partial \ln T}{\partial \ln P} \right)_S$$

$$\kappa_K \propto \rho T^{-3.5}$$

Thin Outer Radiative Zone
with H^- ,

$$\kappa_{H^-} \propto Z \rho^{0.5} T^9$$

$$\kappa_p P_p = \frac{2}{3} g$$

Pre-Main Sequence Evolution

Convective and Radiative Contraction

Table 8.1 Evolutionary times (years)

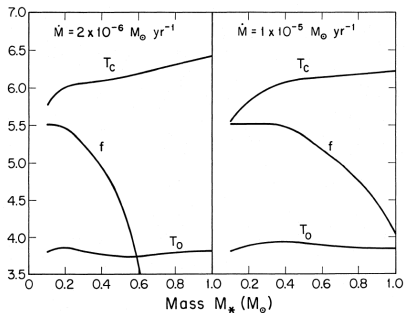
Mass (M_{\odot})	Pre-main-sequence time	Mass (M_{\odot})	Pre-main-sequence time
0.1	1.2×10^9	1.2	3.4×10^7
0.2	5.1×10^8	1.4	1.6×10^7
0.3	3.8×10^8	1.6	1.1×10^7
0.4	2.3×10^8	1.8	9.0×10^6
0.5	1.5×10^8	2.0	7.0×10^6
0.6	1.0×10^8	2.5	4.0×10^6
0.7	7.5×10^7	3.0	2.0×10^6
0.8	6.5×10^7	4.0	5.0×10^5
0.9	5.5×10^7	5.0	2.0×10^5
1.0	4.0×10^7	6.0	1.0×10^5

Bodenheimer, 2011

Stars above $6M_{\odot}$ are already in the main sequence when the accretion phase is over.

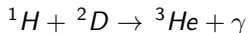
Pre-Main Sequence Evolution

Deuterium Burning and the Stellar Birthline



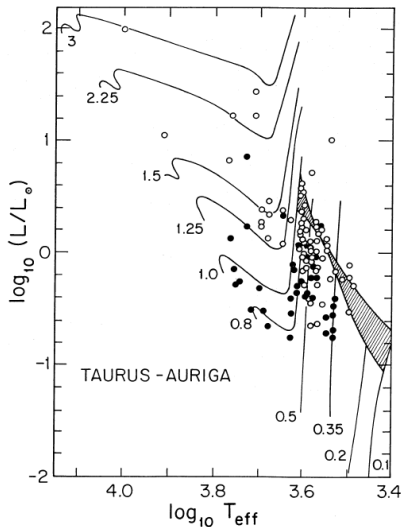
Stahler, 1988

Deuterium Burns at 10^6 K



$$\epsilon \propto f [D/H] \rho T^{11.8}$$

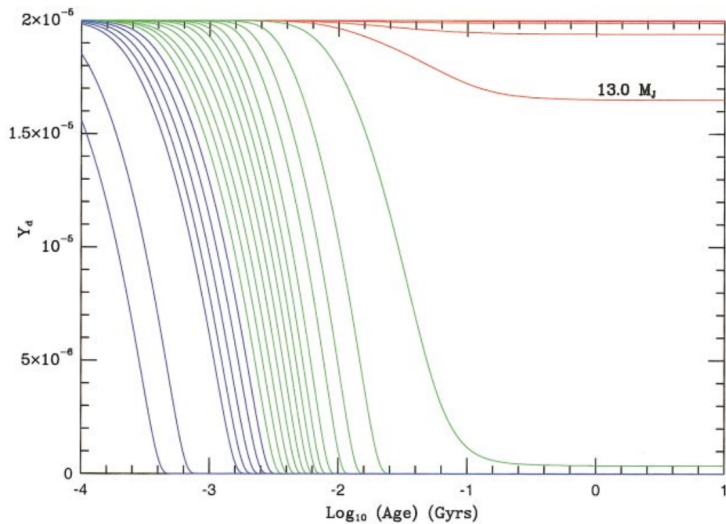
$$[D/H] = 2 \times 10^{-5}, f = 1$$



Stahler, 1988

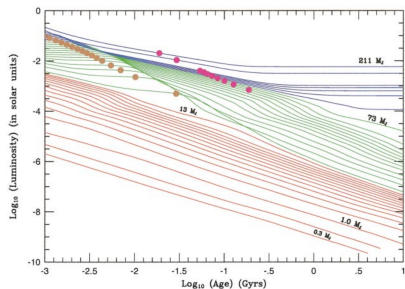
Pre-Main Sequence Evolution

Deuterium Burning and the Stellar Birthline



Pre-Main Sequence Evolution

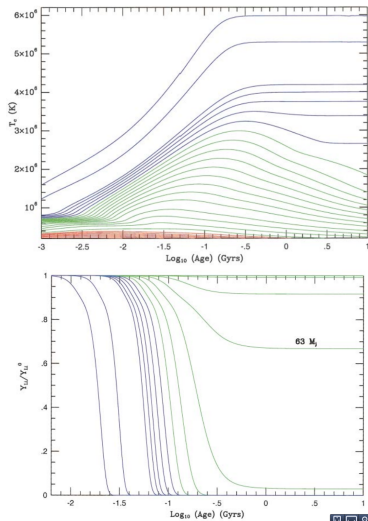
Lithium Burning and Substellar Objects



Burrows et al., 2003

Cores with $M < 0.08M_{\odot}$, can't burn Hydrogen

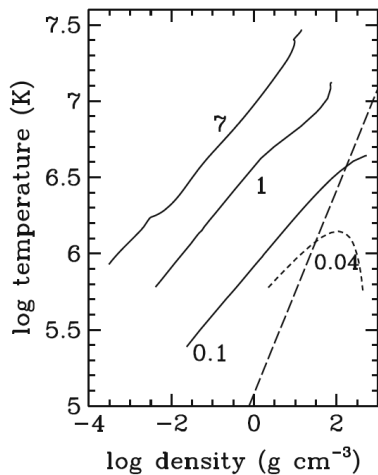
Lithium Burns at 2.5×10^6 K
 ${}^1\text{H} + {}^7\text{Li} \rightarrow {}^4\text{He} + {}^4\text{He}$



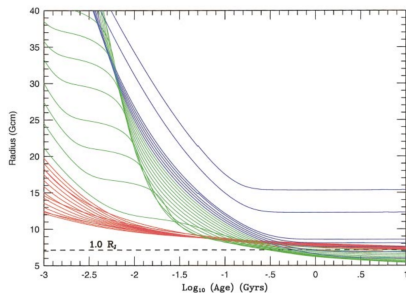
Burrows et al., 2003

Pre-Main Sequence Evolution

Degeneracy



Bodenheimer, 2011



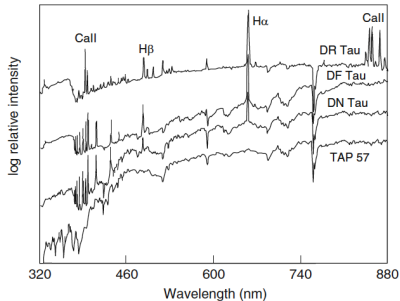
Burrows et al., 2003

$$P_e = 1.004 \times 10^{13} (\rho/\mu_e)^{5/3} \text{ dyne cm}^{-2}$$

$$\rho = 2.4 \times 10^{-8} \mu_e T^{3/2} \text{ g cm}^{-3}$$

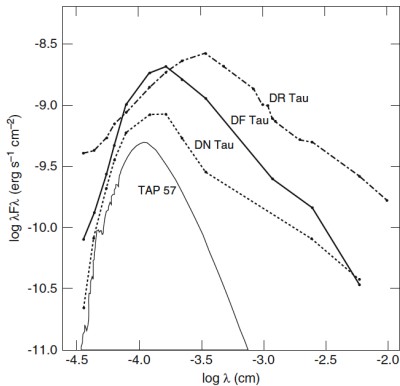
Pre-Main Sequence Evolution

T Tauri Stars



Lada et al., 1999

H α , high *Li* abundance ($\sim 10^{-9} H$), nearby dark clouds, X-rays emission, strong magnetic fields (Zeeman splitting \sim kilogauss).

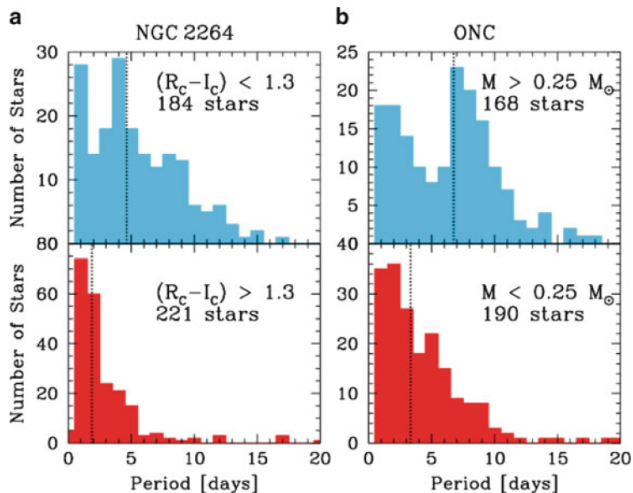


Lada et al., 1999

Infrared excess in CTTS, due to dusty disk.

Pre-Main Sequence Evolution

T Tauri Stars



Lamm et al., 2005

Contraction, magnetic star disk interaction, stellar winds.

Conclusions

We have made a lot of progress in understanding the protostar and pre-main sequence phase of star formation.

Many challenges remain: The luminosity problem, the role of magnetic fields, star disk interaction, stellar winds.

References

Stahler, S. W., ApJ 332, pp. 804, 1988.

Palla, F., Stahler, S., ApJ 525, pp. 772, 1999.

Burrows, A., Hubbard, W., Lunine, J., Liebert, J., Rev. of Modern Physics 73, pp. 719, 2001.

Bodenheimer, Principles of Star Formation, Springer, 2011.